Field Due to an Electric Dipole  An electric dipole consists of two particles with charges of equal magnitude $q$ but opposite sign, separated by a small distance $d$. Their electric dipole moment $\vec{p}$ has magnitude $qd$ and points from the negative charge to the positive charge. The magnitude of the electric field set up by the dipole at a distant point on the dipole axis (which runs through both charges) is

$$E = \frac{1}{2\pi\varepsilon_0} \frac{p}{z^3},$$  \hspace{1cm} (22.9)

where $z$ is the distance between the point and the center of the dipole.

Field Due to a Continuous Charge Distribution  The electric field due to a continuous charge distribution is found by treating charge elements as point charges and then summing, via integration, the electric field vectors produced by all the charge elements.

**Questions**

1. Figure 22-21 shows three arrangements of electric field lines. In each arrangement, a proton is released from rest at point $A$ and is then accelerated through point $B$ by the electric field. Points $A$ and $B$ have equal separations in the three arrangements. Rank the arrangements according to the linear momentum of the proton at point $B$, greatest first.

![FIG. 22-21](image)

2. Figure 22-22 shows four situations in which four charged particles are evenly spaced to the left and right of a central point. The charge values are indicated. Rank the situations according to the magnitude of the net electric field at the central point, greatest first.

![FIG. 22-22](image)

3. Figure 22-23 shows two charged particles fixed in place on an axis. (a) Where on the

![FIG. 22-23](image)

4. Figure 22-24 shows two square arrays of charged particles. The squares, which are centered on point $P$, are misaligned. The particles are separated by either $d$ or $d/2$ along the perimeters of the squares. What are the magnitude and direction of the net electric field at $P$?

![FIG. 22-24](image)

5. In Fig. 22-25, two particles of charge $-q$ are arranged symmetrically about the $y$ axis; each produces an electric field at point $P$ on that axis. (a) Are the magnitudes of the fields at $P$ equal? (b) Is each electric field directed toward or away from the charge producing it? (c) Is the magnitude of the net electric field at $P$ equal to the sum of the magnitudes $E$ of the two field vectors (is it equal to $2E$)? (d) Do the $x$ components of those two field vectors add or cancel? (e) Do their $y$ components add or cancel? (f) Is the direction of the net field at $P$ that of the canceling components or
the adding components? (g) What is the direction of the net field?

6 In Fig. 22-26, an electron e travels through a small hole in plate A and then toward plate B. A uniform electric field in the region between the plates then slows the electron without deflecting it. (a) What is the direction of the field? (b) Four other particles similarly travel through small holes in either plate A or plate B and then into the region between the plates. Three have charges +q1, +q2, and −q3. The fourth (labeled n) is a neutron, which is electrically neutral. Does the speed of each of those four other particles increase, decrease, or remain the same in the region between the plates?

7 In Fig. 22-27a, a circular plastic rod with uniform charge +Q produces an electric field of magnitude E at the center of curvature (at the origin). In Figs. 22-27b, c, and d, more circular rods, each with identical uniform charges +Q, are added until the circle is complete. A fifth arrangement (which would be labeled e) is like that in d except the rod in the fourth quadrant has charge −Q. Rank the five arrangements according to the magnitude of the electric field at the center of curvature, greatest first.

8 In Fig. 22-28, two identical circular nonconducting rings are centered on the same line. For three situations, the uniform charges on rings A and B are, respectively, (1) q0 and q0, (2) −q0 and −q0, and (3) −q0 and q0. Rank the situations according to the magnitude of the net electric field at (a) point P1 midway between the rings, (b) point P2 at the center of ring B, and (c) point P3 to the right of ring B, greatest first.

9 The potential energies associated with four orientations of an electric dipole in an electric field are (1) −5U0, (2) −7U0, (3) 3U0, and (4) 5U0, where U0 is positive. Rank the orientations according to (a) the angle between the electric dipole moment p and the electric field E and (b) the magnitude of the torque on the electric dipole, greatest first.

10 (a) In Checkpoint 4, if the dipole rotates from orientation 1 to orientation 2, is the work done on the dipole by the field positive, negative, or zero? (b) If, instead, the dipole rotates from orientation 1 to orientation 4, is the work done by the field more than, less than, or the same as in (a)?

11 Figure 22-29 shows two disks and a flat ring, each with the same uniform charge Q. Rank the objects according to the magnitude of the electric field they create at points P (which are at the same vertical heights), greatest first.

PROBLEMS

sec. 22-3 Electric Field Lines

1 In Fig. 22-30 the electric field lines on the left have twice the separation of those on the right. (a) If the magnitude of the field at A is 40 N/C, what is the magnitude of the force on a proton at A? (b) What is the magnitude of the field at B?

2 Sketch qualitatively the electric field lines both between and outside two concentric conducting spherical shells when a uniform positive charge q1 is on the inner shell and a uniform negative charge −q2 is on the outer. Consider the cases q1 > q2, q1 = q2, and q1 < q2.

sec. 22-4 The Electric Field Due to a Point Charge

3 What is the magnitude of a point charge whose electric field 50 cm away has the magnitude 2.0 N/C? SSM

4 What is the magnitude of a point charge that would create an electric field of 1.00 N/C at points 1.00 m away?

5 The nucleus of a plutonium-239 atom contains 94 pro...
tons. Assume that the nucleus is a sphere with radius 6.64 fm and with the charge of the protons uniformly spread through the sphere. At the nucleus surface, what are the (a) magnitude and (b) direction (radially inward or outward) of the electric field produced by the protons? SSM

**6** Two particles are fixed to an x axis: particle 1 of charge $-2.00 \times 10^{-7}$ C at $x = 6.00$ cm and particle 2 of charge $+2.00 \times 10^{-7}$ C at $x = 21.0$ cm. Midway between the particles, what is their net electric field in unit-vector notation?

**7** Two particles are fixed to an x axis: particle 1 of charge $q_1 = 2.1 \times 10^{-8}$ C at $x = 20$ cm and particle 2 of charge $q_2 = -4.00q_1$ at $x = 70$ cm. At what coordinate on the axis is the net electric field produced by the particles equal to zero? SSM

**8** In Fig. 22-31, particle 1 of charge $q_1 = -5.00g$ and particle 2 of charge $q_2 = +2.00q_2$ are fixed to an x axis. (a) As a multiple of distance $L$, at what coordinate on the axis is the net electric field of the particles zero? (b) Sketch the net electric field lines.

**9** In Fig. 22-32, the four particles form a square of edge length $a = 5.00$ cm and have charges $q_1 = +10.0$ nC, $q_2 = -20.0$ nC, $q_3 = +20.0$ nC, and $q_4 = -10.0$ nC. In unit-vector notation, what net electric field do the particles produce at the square’s center? SSM

**10** In Fig. 22-33, the four particles are fixed in place and have charges $q_1 = q_2 = +5e$, $q_3 = +3e$, and $q_4 = -12e$. Distance $d = 5.0$ µm. What is the magnitude of the net electric field at point $P$ due to the particles?

**11** Figure 22-34 shows two charged particles on an x axis: $-q = -3.20 \times 10^{-19}$ C at $x = -3.00$ m and $q = 3.20 \times 10^{-19}$ C at $x = +3.00$ m. What are the (a) magnitude and (b) direction (relative to the positive direction of the x axis) of the net electric field produced at point $P$ at $y = 4.00$ m?

**12** Figure 22-35a shows two charged particles fixed in place on an x axis with separation $L$. The ratio $q_1/q_2$ of their charge magnitudes is 4:1. Figure 22-35b shows the x component $E_{net,x}$ of their net electric field along the x axis just to the right of particle 2. The x axis scale is set by $x_p = 30.0$ cm. (a) At what value of $x > 0$ is $E_{net,x}$ maximum? (b) If particle 2 has charge $-q_2 = -3e$, what is the value of that maximum?

![FIG. 22-31 Problem 8.](image1)

![FIG. 22-32 Problem 9.](image2)

![FIG. 22-33 Problem 10.](image3)

**FIG. 22-34 Problem 11.**

**FIG. 22-35** Problem 12.

**13** In Fig. 22-36, the three particles are fixed in place and have charges $q_1 = q_2 = +e$ and $q_3 = +2e$. Distance $a = 6.00 \mu$m. What are the (a) magnitude and (b) direction of the net electric field at point $P$ due to the particles?

**14** Figure 22-37 shows an uneven arrangement of electrons (e) and protons (p) on a circular arc of radius $r = 2.00$ cm, with angles $\theta_1 = 30.0^\circ$, $\theta_2 = 50.0^\circ$, $\theta_3 = 30.0^\circ$, and $\theta_4 = 20.0^\circ$. What are the (a) magnitude and (b) direction (relative to the positive direction of the x axis) of the net electric field produced at the center of the arc?

**15** Figure 22-38 shows a proton (p) on the central axis through a disk with a uniform charge density due to excess electrons. Three of those electrons are shown: electron $e_1$ at the disk center and electrons $e_2$ at opposite sides of the disk, at radius $R$ from the center. The proton is initially at distance $z = R = 2.00$ cm from the disk. At that location, what are the magnitudes of (a) the electric field $E_z$ due to electron $e_1$, and (b) the net electric field $E_{net}$ due to electrons $e_2$? The proton is then moved to $z = R/10.0$. What then are the magnitudes of (c) $E_z$ and (d) $E_{net}$ at the proton’s location? (e) From (a) and (c) we see that as the proton gets nearer to the disk, the magnitude of $E_z$ increases. Why does the magnitude of $E_{net}$ decrease, as we see from (b) and (d)?

**16** Figure 22-39 shows a plastic ring of radius $R = 50.0$ cm. Two small charged beads are on the ring: Bead 1 of charge $+2.00 \mu$C is fixed in place at the left side; bead 2 of charge $+6.00 \mu$C can be moved along the ring. The two beads produce a net electric field of magnitude $E$ at the center of the ring. At what (a) positive and (b) negative value of angle $\theta$ should bead 2 be positioned such that $E = 2.00 \times 10^5$ N/C?
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**Problem 17** Two charged beads are on the plastic ring in Fig. 22-40a. Bead 2, which is not shown, is fixed in place on the ring, which has radius $R = 60.0$ cm. Bead 1 is initially on the x axis at angle $\theta = 0^\circ$. It is then moved to the opposite side, at angle $\theta = 180^\circ$, through the first and second quadrants of the xy coordinate system. Figure 22-40b gives the x component of the net electric field produced at the origin by the two beads as a function of $\theta$, and Fig. 22-40c gives the y component. The vertical axis scales are set by $E_{\text{max}} = 5.0 \times 10^4$ N/C and $E_{\text{max}} = -9.0 \times 10^4$ N/C. (a) At what angle $\theta$ is bead 2 located? What are the charges of (b) bead 1 and (c) bead 2?

![Fig. 22-40](image)

**Problem 17**

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**Problem 21** Electric quadrupole. Figure 22-42 shows an electric quadrupole. It consists of two dipoles with dipole moments that are equal in magnitude but opposite in direction. Show that the value of $E$ on the axis of the quadrupole for a point $P$ a distance $z$ from its center (assume $z \gg d$) is given by

$$E = \frac{3Q}{4\pi\varepsilon_0 z^4},$$

in which $Q (= 2qd^3)$ is known as the quadrupole moment of the charge distribution.

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**Section 22-6 The Electric Field Due to a Line of Charge**

**Problem 22** Density, density, density. (a) A charge $-300e$ is uniformly distributed along a circular arc of radius 4.00 cm, which subtends an angle of 40°. What is the linear charge density along the arc? (b) A charge $-300e$ is uniformly distributed over one face of a circular disk of radius 2.00 cm. What is the surface charge density over that face? (c) A charge $-300e$ is uniformly distributed over the surface of a sphere of radius 2.00 cm. What is the surface charge density over that surface?

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**Problem 23** Figure 22-43 shows two parallel nonconducting rings with their central axes along a common line. Ring 1 has uniform charge $q_1$ and radius $R$; ring 2 has uniform charge $q_2$ and the same radius $R$. The rings are separated by distance $d = 3.00R$. The net electric field at point $P$ on the common line, at distance $R$ from ring 1, is zero. What is the ratio $q_2/q_1$?

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**Problem 24** In Fig. 22-44, a thin glass rod forms a semicircle of radius $r = 5.00$ cm. Charge is uniformly distributed along the rod, with $+q = 4.50$ pC in the upper half and $-q = -4.50$ pC in the lower half. What are the $x$ and $y$ components of the electric field at $P$, the center of the semicircle?

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**Problem 25** In Fig. 22-45, two curved plastic rods, one of charge $+q$ and the other of charge $-q$, form a circle of radius $R = 8.50$ cm in an $xy$ plane. The $x$ axis passes through both of the connecting points, and the charge is distributed uniformly on both rods. If $q = 15.0$ pC, what are the $x$ and $y$ components of the electric field produced at $P$, the center of the circle?

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**Problem 26** Charge is uniformly distributed around a ring of radius $R = 2.40$ cm, and the resulting electric field magnitude $E$ is measured along the ring’s central axis (perpendicular to the plane of
the ring). At what distance from the ring's center is $E$ maximum?

**27** In Fig. 22-46, a nonconducting rod of length $L = 8.15$ cm has charge $-q = -4.23$ fC uniformly distributed along its length. (a) What is the linear charge density of the rod? What are the (b) magnitude and (c) direction (relative to the positive direction of the $x$ axis) of the electric field produced at point $P$, at distance $a = 12.0$ cm from the rod? What is the electric field magnitude produced at distance $a = 50$ m by (d) the rod and (e) a particle of charge $-q = -4.23$ fC that replaces the rod?

**28** Figure 22-47 shows two concentric rings, of radii $R$ and $R' = 3.00R$, that lie on the same plane. Point $P$ lies on the central $z$ axis, at distance $D = 2.00R$ from the center of the rings. The smaller ring has uniformly distributed charge $+Q$. In terms of $Q$, what is the uniform distributed charge on the larger ring if the net electric field at $P$ is zero?

**29** Figure 22-48 shows three circular arcs centered on the origin of a coordinate system. On each arc, the uniformly distributed charge is given in terms of $Q = 2.00 \mu$C. The radii are given in terms of $R = 10.0$ cm. What are the (a) magnitude and (b) direction (relative to the positive $x$ direction) of the net electric field at the origin due to the arcs?

**30** A thin nonconducting rod with a uniform distribution of positive charge $Q$ is bent into a circle of radius $R$ (Fig. 22-49). The central perpendicular axis through the ring is a $z$ axis, with the origin at the center of the ring. What is the magnitude of the electric field due to the rod at (a) $z = 0$ and (b) $z = \infty$? (c) In terms of $R$, at what positive value of $z$ is that magnitude maximum? (d) If $R = 2.00$ cm and $Q = 4.00 \mu$C, what is the maximum magnitude?

**31** Figure 22-50a shows a nonconducting rod with a uniformly distributed charge $+Q$. The rod forms a half-circle with radius $R$ and produces an electric field of magnitude $E_{arc}$ at its center of curvature $P$. If the arc is collapsed to a point at distance $R$ from $P$ (Fig. 22-50b), by what factor is the magnitude of the electric field at $P$ multiplied?

**32** In Fig. 22-51, positive charge $q = 7.81$ PC is spread uniformly along a thin nonconducting rod of length $L = 14.5$ cm. What are the (a) magnitude and (b) direction (relative to the positive direction of the $x$ axis) of the electric field produced at point $P$, at distance $R = 6.00$ cm from the rod along its perpendicular bisector?

**33** In Fig. 22-52, a “semi-infinite” nonconducting rod (that is, infinite in one direction only) has uniform linear charge density $\lambda$. Show that the electric field $E_\|$, at point $P$ makes an angle of $45^\circ$ with the rod and that this result is independent of the distance $R$. (Hint: Separately find the component of $E_\parallel$ parallel to the rod and the component perpendicular to the rod.)

**sec. 22-7 The Electric Field Due to a Charged Disk**

**34** A disk of radius 2.5 cm has a surface charge density of 3.8 $\mu$C/m$^2$ on its upper face. What is the magnitude of the electric field produced by the disk at a point on its central axis at distance $z = 12$ cm from the disk?

**35** At what distance along the central perpendicular axis of a uniformly charged plastic disk of radius 0.600 m is the magnitude of the electric field equal to one-half the magnitude of the field at the center of the surface of the disk?

**36** Figure 22-53a shows a circular disk that is uniformly charged. The central $z$ axis is perpendicular to the disk face, with the origin at the disk. Figure 22-53b gives the magnitude of the electric field along that axis in terms of the maximum magnitude $E_{max}$ at the disk surface. The $z$ axis scale is set by $z_i = 8.0$ cm. What is the radius of the disk?

**37** Suppose you design an apparatus in which a uniformly charged disk of radius $R$ is to produce an electric field. The field magnitude is most important along the central perpendicular axis of the disk, at a point $P$ at distance 2.00R from the disk (Fig. 22-54a). Cost analysis suggests that you
switch to a ring of the same outer radius $R$ but with inner radius $R/2.00$ (Fig. 22-54b). Assume that the ring will have the same surface charge density as the original disk. If you switch to the ring, by what percentage will you decrease the electric field magnitude at $P$?

- **38** A circular plastic disk with radius $R = 2.00$ cm has a uniformly distributed charge $Q = + (2.00 \times 10^6) \text{e}$ on one face. A circular ring of width $30 \mu\text{m}$ is centered on that face, with the center of that width at radius $r = 0.50$ cm. In coulombs, what charge is contained within the width of the ring?

**sec. 22-8 A Point Charge in an Electric Field**

- **39** An electron is released from rest in a uniform electric field of magnitude $2.00 \times 10^4 \text{ N/C}$. Calculate the acceleration of the electron. (Ignore gravitation.)

- **40** An electron is accelerated eastward at $1.80 \times 10^9 \text{ m/s}^2$ by an electric field. Determine the (a) magnitude and (b) direction of the electric field.

- **41** An electron on the axis of an electric dipole is 25 nm from the center of the dipole. What is the magnitude of the electrostatic force on the electron if the dipole moment is $3.6 \times 10^{-29} \text{ C} \cdot \text{m}$? Assume that 25 nm is much larger than the dipole charge separation.

- **42** An alpha particle (the nucleus of a helium atom) has a mass of $6.64 \times 10^{-27} \text{ kg}$ and a charge of $+2e$. What are the (a) magnitude and (b) direction of the electric field that will balance the gravitational force on the particle?

- **43** A charged cloud system produces an electric field in the air near Earth's surface. A particle of charge $-2.0 \times 10^{-9} \text{ C}$ is acted on by a downward electrostatic force of $3.0 \times 10^{-6} \text{ N}$ when placed in this field. (a) What is the magnitude of the electric field? What are the (b) magnitude and (c) direction of the electrostatic force $F_E$ on the proton placed in this field? (d) What is the magnitude of the gravitational force $F_g$ on the proton? (e) What is the ratio $F_E/F_g$ in this case?

- **44** Humid air breaks down (its molecules become ionized) in an electric field of $3.0 \times 10^6 \text{ N/C}$. In that field, what is the magnitude of the electrostatic force on (a) an electron and (b) an ion with a single electron missing?

- **45** Beams of high-speed protons can be produced in "guns" using electric fields to accelerate the protons. (a) What acceleration would a proton experience if the gun's electric field were $2.00 \times 10^4 \text{ N/C}$? (b) What speed would the proton attain if the field accelerated the proton through a distance of 1.00 cm?

- **46** An electron with a speed of $5.00 \times 10^6 \text{ cm/s}$ enters an electric field of magnitude $1.00 \times 10^3 \text{ N/C}$, traveling along a field line in the direction that retards its motion. (a) How far will the electron travel in the field before stopping momentarily, and (b) how much time will have elapsed? (c) If the region containing the electric field is 8.00 mm long (too short for the electron to stop within it), what fraction of the electron's initial kinetic energy will be lost in that region?

- **47** In Millikan’s experiment, an oil drop of radius $1.64 \mu\text{m}$ and density $0.851 \text{ g/cm}^3$ is suspended in chamber C (Fig. 22-14) when a downward electric field of $1.92 \times 10^3 \text{ N/C}$ is applied. Find the charge on the drop, in terms of $e$.

- **48** At some instant the velocity components of an electron moving between two charged parallel plates are $v_x = 1.5 \times 10^5 \text{ m/s}$ and $v_y = 3.0 \times 10^3 \text{ m/s}$. Suppose the electric field between the plates is given by $E = (120 \text{ N/C})$. In unit-vector notation, what are (a) the electron’s acceleration in that field and (b) the electron’s velocity when its $x$ coordinate has changed by 2.0 cm?

- **49** A uniform electric field exists in a region between two oppositely charged plates. An electron is released from rest at the surface of the negatively charged plate and strikes the surface of the opposite plate, 2.0 cm away, in a time $1.5 \times 10^{-8}$ s. (a) What is the speed of the electron as it strikes the second plate? (b) What is the magnitude of the electric field $E$?

- **50** In Fig. 22-55, an electron is shot at an initial speed of $v_0 = 2.00 \times 10^6 \text{ m/s}$, at angle $\theta_0 = 40.0^\circ$ from an $x$ axis. It moves through a uniform electric field $E = (5.00 \text{ N/C})$. A screen for detecting electrons is positioned parallel to the $y$ axis, at distance $x = 3.00$ m. In unit-vector notation, what is the velocity of the electron when it hits the screen?

- **51** Two large parallel copper plates are 5.0 cm apart and have a uniform electric field between them as depicted in Fig. 22-56. An electron is released from the negative plate at the same time that a proton is released from the positive plate. Neglect the force of the particles on each other and find their distance from the positive plate when they pass each other. (Does it surprise you that you need not know the electric field to solve this problem?)

- **52** In Fig. 22-57, an electron (e) is to be released from rest on the central axis of a uniformly charged disk of radius $R$. The surface charge density on the disk is $+4.00 \mu\text{C/m}^2$. What is the magnitude of the electron’s initial acceleration if it is released at a distance (a) $R$, (b) $R/100$, and (c) $R/1000$ from the center of the disk? (d) Why does the acceleration magnitude increase only slightly as the release point is moved closer to the disk?

- **53** A 10.0 g block with a charge of $-8.00 \times 10^{-3} \text{ C}$ is placed in an electric field $E = (3000\text{i} - 600\text{j}) \text{ N/C}$. What are the (a) magnitude and (b) direction (relative to the positive direction of the x axis) of the electrostatic force on the block? If the block is released from rest at the origin at time $t = 0$, what are its (c) x and (d) y coordinates at $t = 3.00  \text{s}$?

- **54** An electron enters a region of uniform electric field with an initial velocity of 40 km/s in the same direction as the electric field, which has magnitude $E = 50 \text{ N/C}$. (a) What is the speed of the electron 1.5 ns after entering this region? (b) How far does the electron travel during the 1.5 ns interval?

- **55** Assume that a honeybee is a sphere of diameter 1.00 cm with a charge of +45.0 pC uniformly spread over its surface.
sec. 22-9 A Dipole in an Electric Field

56 An electric dipole consists of charges +2e and −2e separated by 0.78 nm. It is in an electric field of strength 3.4 × 10^6 N/C. Calculate the magnitude of the torque on the dipole when the dipole moment is (a) parallel to, (b) perpendicular to, and (c) antiparallel to the electric field.

57 An electric dipole consisting of charges of magnitude 1.50 nC separated by 6.20 μm is in an electric field of strength 1100 N/C. What are (a) the magnitude of the electric field moment and (b) the difference between the potential energies for dipole orientations parallel and antiparallel to \( \vec{E} \)?

58 A certain electric dipole is placed in a uniform electric field \( \vec{E} \) of magnitude 40 N/C. Figure 22-58 gives the magnitude \( \tau \) of the torque on the dipole versus the angle \( \theta \) between field \( \vec{E} \) and the dipole moment \( \vec{p} \). The vertical axis scale is set by \( \tau_1 = 100 \times 10^{-28} \) N⋅m. What is the magnitude of \( \vec{p} \)?

59 Find an expression for the oscillation frequency of an electric dipole of dipole moment \( \vec{p} \) and rotational inertia \( I \) for small amplitudes of oscillation about its equilibrium position in a uniform electric field of magnitude \( E \).

60 A certain electric dipole is placed in a uniform electric field \( \vec{E} \) of magnitude 20 N/C. Figure 22-59 gives the potential energy \( U \) of the dipole versus the angle \( \theta \) between field \( \vec{E} \) and the dipole moment \( \vec{p} \). The vertical axis scale is set by \( U_j = 100 \times 10^{-28} \) J. What is the magnitude of \( \vec{p} \)?

61 How much work is required to turn an electric dipole 180° in a uniform electric field of magnitude \( E = 46.0 \) N/C if \( p = 3.02 \times 10^{-25} \) C⋅m and the initial angle is 64°?

Additional Problems

62 In one of his experiments, Millikan observed that the following measured charges, among others, appeared at different times on a single drop:

\[
\begin{align*}
6.563 \times 10^{-19} \text{ C} & \quad 13.13 \times 10^{-19} \text{ C} & \quad 19.71 \times 10^{-19} \text{ C} \\
8.204 \times 10^{-19} \text{ C} & \quad 16.48 \times 10^{-19} \text{ C} & \quad 22.89 \times 10^{-19} \text{ C} \\
11.50 \times 10^{-19} \text{ C} & \quad 18.08 \times 10^{-19} \text{ C} & \quad 26.13 \times 10^{-19} \text{ C}
\end{align*}
\]

What value for the elementary charge \( e \) can be deduced from these data?

63 In Fig. 22-60a, a particle of charge \( +Q \) produces an electric field of magnitude \( E_{\text{part}} \) at point \( P \), at distance \( R \) from the particle. In Fig. 22-60b, that same amount of charge is spread uniformly along a circular arc that has radius \( R \) and subtends an angle \( \theta \). The charge on the arc produces an electric field of magnitude \( E_{\text{arc}} \) at its center of curvature \( P \). For what value of \( \theta \) does \( E_{\text{arc}} = 0.500 E_{\text{part}} \)? (Hint: You will probably resort to a graphical solution.)

64 In Fig. 22-61, eight particles form a square in which distance \( d = 2.0 \) cm. The charges are \( q_1 = +3e \), \( q_2 = +e \), \( q_3 = -5e \), \( q_4 = -2e \), \( q_5 = +3e \), \( q_6 = +e \), \( q_7 = -5e \), and \( q_8 = +e \). In unit-vector notation, what is the net electric field do the particles produce at the square's center?

65 Two particles, each with a charge of magnitude 12 nC, are at two of the vertices of an equilateral triangle with edge length 2.0 m. What is the magnitude of the electric field at the third vertex if (a) both charges are positive and (b) one charge is positive and the other is negative?

66 Three particles, each with positive charge \( Q \), form an equilateral triangle, with each side of length \( d \). What is the magnitude of the electric field produced by the particles at the midpoint of any side?

67 A particle of charge \( -q_1 \) is at the origin of an x axis. (a) At what location on the axis should a particle of charge \( -4q_1 \) be placed so that the net electric field is zero at \( x = 2.0 \) mm on the axis? (b) If, instead, a particle of charge \( +4q_1 \) is placed at that location, what is the direction (relative to the positive direction of the x axis) of the net electric field at \( x = 2.0 \) mm?

68 A proton and an electron form two corners of an equilateral triangle of side length \( 2.0 \times 10^{-6} \) m. What is the magnitude of the net electric field these two particles produce at the third corner?

69 In Fig. 22-62, particle 1 (of charge \( +1.00 \) μC), particle 2 (of charge \( -1.00 \) μC), and particle 3 (of charge \( Q \)) form an equilateral triangle of edge length \( a \). For what value of \( Q \) (both sign and magnitude) does the net electric field produced by the particles at the center of the triangle vanish?

70 (a) What total (excess) charge \( q \) must the disk in Fig. 22-13 have for the electric field on the surface of the disk at its center to have magnitude \( 3.0 \times 10^6 \) N/C, the \( E \) value at which air breaks down electrically, producing sparks? Take the disk radius as 2.5 cm, and use the listing for air in Table 22-1.

(b) Suppose each surface atom has an effective cross-sectional area of 0.015 nm². How many atoms are needed to make up...
the disk surface? (c) The charge calculated in (a) results from some of the surface atoms having one excess electron. What fraction of these atoms must be so charged?

71 A spherical water drop 1.20 \( \mu \text{m} \) in diameter is suspended in calm air due to a downward-directed atmospheric electric field of magnitude \( E = 462 \text{ N/C} \). (a) What is the magnitude of the gravitational force on the drop? (b) How many excess electrons does it have?

72 In Fig. 22-63, an electric dipole swings from an initial orientation \( i (\theta_i = 20.0^\circ) \) to a final orientation \( f (\theta_f = 20.0^\circ) \) in a uniform external electric field \( \vec{E} \). The electric dipole moment is \( 1.60 \times 10^{-31} \text{ C \cdot m} \); the field magnitude is \( 3.00 \times 10^6 \text{ N/C} \). What is the change in the dipole’s potential energy?

73 A charge of 20 nC is uniformly distributed along a straight rod of length 4.0 m that is bent into a circular arc with a radius of 2.0 m. What is the magnitude of the electric field at the center of curvature of the arc?

74 (a) What is the magnitude of an electron’s acceleration in a uniform electric field of magnitude \( 1.40 \times 10^6 \text{ N/C} \)? (b) How long would the electron take, starting from rest, to attain one-tenth the speed of light? (c) How far would it travel in that time?

75 A clock face has negative point charges \(-q, -2q, -3q, \ldots, -12q\) fixed at the positions of the corresponding numerals. The clock hands do not perturb the net field due to the point charges. At what time does the hour hand point in the same direction as the electric field vector at the center of the dial? (Hint: Use symmetry.)

76 An electron is constrained to the central axis of the ring of charge of radius \( R \) in Fig. 22-10, with \( z \ll R \). Show that the electrostatic force on the electron can cause it to oscillate through the ring center with an angular frequency

\[
\omega = \sqrt{\frac{eq}{4\pi\varepsilon_0 m R^3}},
\]

where \( q \) is the ring’s charge and \( m \) is the electron’s mass.

77 An electric field \( \vec{E} \) with an average magnitude of about 150 N/C points downward in the atmosphere near Earth’s surface. We wish to “float” a sulfur sphere weighing 4.4 N in this field by charging the sphere. (a) What charge (both sign and magnitude) must be used? (b) Why is the experiment impractical?

78 Calculate the electric dipole moment of an electron and a proton 4.30 nm apart.

79 The electric field in an \( xy \) plane produced by a positively charged particle is \( 7.2\times(4.0i + 3.0j) \text{ N/C} \) at the point \( (3.0, 3.0) \text{ cm} \) and 100i N/C at the point \( (2.0, 0) \text{ cm} \). What are the (a) \( x \) and (b) \( y \) coordinates of the particle? (c) What is the charge of the particle? SSM

80 A circular rod has a radius of curvature \( R = 9.00 \text{ cm} \) and a uniformly distributed positive charge \( Q = 6.25 \text{ pC} \) and subtends an angle \( \theta = 2.40 \text{ rad} \). What is the magnitude of the electric field that \( Q \) produces at the center of curvature?

81 An electric dipole with dipole moment

\[
\vec{p} = (3.00i + 4.00j)(1.24 \times 10^{-30} \text{ C \cdot m})
\]
is in an electric field \( \vec{E} = (4000 \text{ N/C})i \). (a) What is the potential energy of the electric dipole? (b) What is the torque acting on it? (c) If an external agent turns the dipole until its electric dipole moment is

\[
\vec{p} = (-4.00i + 3.00j)(1.24 \times 10^{-30} \text{ C \cdot m}),
\]

how much work is done by the agent? SSM

82 In Fig. 22-62, particle 1 (of charge +2.00 pC), particle 2 (of charge -2.00 pC), and particle 3 (of charge +5.00 pC) form an equilateral triangle of edge length \( a = 9.50 \text{ cm} \). (a) Relative to the positive direction of the \( x \) axis, determine the direction of the force \( \vec{F}_3 \) on particle 3 due to the other particles by sketching electric field lines of the other particles. (b) Calculate the magnitude of force \( \vec{F}_3 \).

83 A charge (uniform linear density = 9.0 nC/m) lies on a string that is stretched along an \( x \) axis from \( x = 0 \) to \( x = 3.0 \text{ m} \). Determine the magnitude of the electric field at \( x = 4.0 \text{ m} \) on the \( x \) axis.

84 Two particles, each of positive charge \( q \), are fixed in place on a \( y \) axis, one at \( y = d \) and the other at \( y = -d \). (a) Write an expression that gives the magnitude \( E \) of the net electric field at points on the \( x \) axis given by \( x = ad \). (b) Graph \( E \) versus \( a \) for the range \( 0 < a < 4 \). From the graph, determine the values of \( a \) that give (c) the maximum value of \( E \) and (d) half the maximum value of \( E \).

85 In Fig. 22-64, particle 1 of charge \( q_1 = 1.00 \text{ pC} \) and particle 2 of charge \( q_2 = -2.00 \text{ pC} \) are fixed at a distance \( d = 5.00 \text{ cm} \) apart. In unit-vector notation, what is the net electric field at points (a) \( A \), (b) \( B \), and (c) \( C \)? (d) Sketch the electric field lines.

86 In Fig. 22-65, a uniform, upward electric field \( \vec{E} \) of magnitude \( 2.00 \times 10^3 \text{ N/C} \) has been set up between two horizontal plates by charging the lower plate positively and the upper plate negatively. The plates have length \( L = 10.0 \text{ cm} \) and separation \( d = 2.00 \text{ cm} \). An electron is then shot between the plates from the left edge of the lower plate. The initial velocity \( \vec{v}_0 \) of the electron makes an angle \( \theta = 45.0^\circ \) with the lower plate and has a magnitude of \( 6.00 \times 10^5 \text{ m/s} \). (a) Will the electron strike one of the plates? (b) If so, which plate and how far horizontally from the left edge will the electron strike?

87 For the data of Problem 62, assume that the charge \( q \) on the drop is given by \( q = ne \), where \( n \) is an integer and \( e \) is the elementary charge. (a) Find \( n \) for each given value of \( q \). (b) Do a linear regression fit of the values of \( q \) versus the values of \( n \) and then use that fit to find \( e \).

88 In Fig. 22-8, let both charges be positive. Assuming \( z \gg d \), show that \( E \) at point \( P \) in that figure is then given by

\[
E = \frac{1}{4\pi\varepsilon_0} \frac{2q}{z^2}.
\]